

Southbourne Infant School

Calculation Policy 2020 - Concrete, Pictorial and Abstract

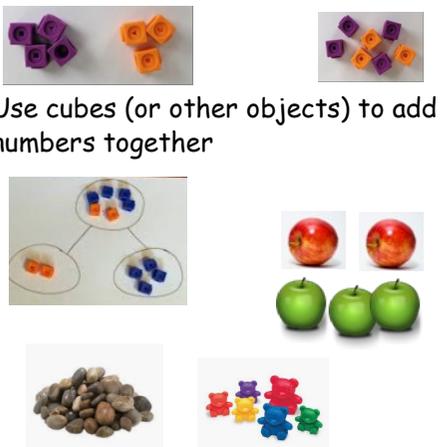
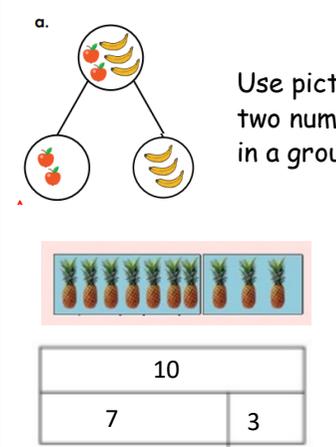
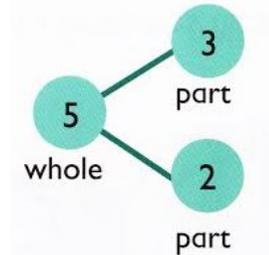
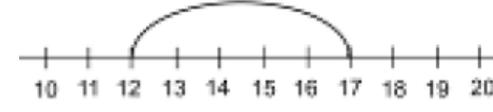
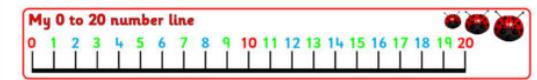
Concrete, Pictorial, Abstract (CPA) is a highly effective approach to teaching that develops a deep and sustainable understanding of maths in pupils.

- **Concrete** is the "doing stage, using concrete objects to model problems.
- **Pictorial** is the "seeing" stage, using representations of objects to model problems. This stage encourages children to make a mental connection between the physical object and abstract levels. This may include looking at pictures, drawing representations or diagrams.
- **Abstract** is the "symbolic" stage, where children are able to use abstract symbols to model problems. Children are introduced to mathematical symbols, for example +, -, x, ÷ to indicate addition, subtraction, multiplication and division.

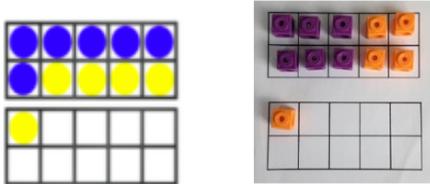
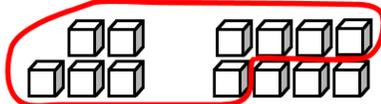
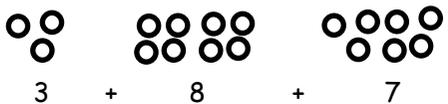
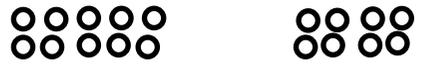
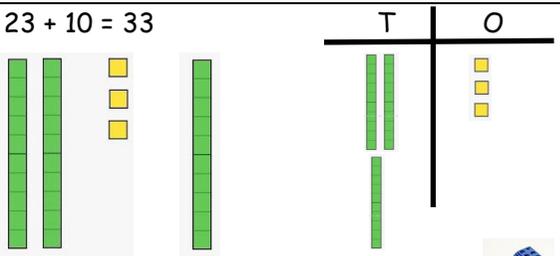
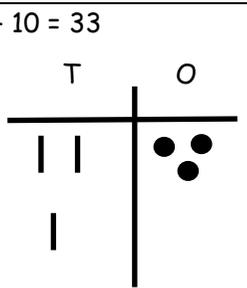


Calculation Policy—Addition

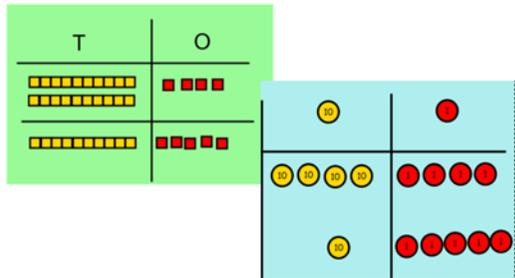
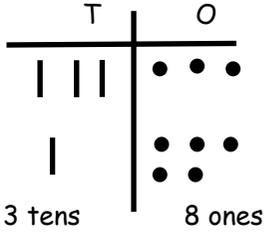
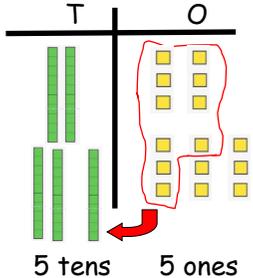
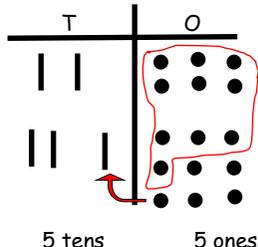
Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as', total, count on.

	Concrete	Pictorial	Abstract
<p>Combining two parts to make a whole .</p> <p>Part-Part Whole</p>	 <p>Use cubes (or other objects) to add two numbers together</p>	<p>a.</p>  <p>Use pictures to add two numbers together in a group or in a bar.</p>	<p>Use a Part-Part Whole diagram to move into the abstract.</p> $3 + 2 = 5$ $2 + 3 = 5$ $5 = 3 + 2$ $5 = 2 + 3$ 
<p>Starting at the bigger number and counting on.</p>	 <p>12.....13, 14, 15, 16, 17.</p> <p>Start with the larger number and count on the small number.</p> <p>4...5, 6.</p> 	 <p>I have 12 marbles. My friend gives me 5 more, how many marbles do I have?</p> <p>Start on 12 on a number line and count on 5 ones.</p> 	$5 + 12 = 17$ <p>Place the larger number in your head and count on the smaller number to find your answer.</p> <p>Remember the larger number may not always be the first number</p>

Calculation Policy—Addition

	Concrete	Pictorial	Abstract
<p>Regrouping to make 10. <i>This is an essential skill for column addition later.</i></p>	<p>Using a tens frame and counters/objects. Start with the bigger number and use the smaller number to make 10.</p> <p>6 and 5</p> 	 <p>Use pictures or a number line. Regroup or partition the smaller number to make 10.</p>	<p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p> <p>$7 + 3 + 1 = 11$</p>
<p>Adding three single digit numbers.</p>	 <p>7 and 3 make 10. 10 and 8 make 18</p>	 <p>$3 + 8 + 7$</p>  <p>$10 + 8 = 18$</p> <p>Draw a picture to recombine the groups to make 10.</p>	<p>Combine the two numbers that make 10 and then add on the rest.</p> <p>$6 + 5 + 4 =$</p> <p>$6 + 4 = 10$ $10 + 5 = 15$</p>
<p>Adding a 2 digit number and a ten or multiple of ten.</p>	<p>$23 + 10 = 33$</p>  <p>Use dienes (tens and ones) or Numicon</p>	<p>$23 + 10 = 33$</p>  <p>Children draw tens and ones grid and then draw sticks and dots to represent the tens and ones.</p>	<p>$23 + 10 = 33$ I know that 10 more than 23 is 33.</p> <p>Introduction of the column method.</p> $\begin{array}{r} 23 \\ + 10 \\ \hline 33 \end{array}$

Calculation Policy—Addition

	Concrete	Pictorial	Abstract
<p>Adding two digit numbers— no regrouping</p>	<p>Add together the ones first then add the tens. Use dienes first before moving onto place value counters</p> <p>$24 + 15 = 38$</p> 	<p>Draw tens and ones grid and then draw sticks and dots to represent the tens and ones. Add the ones and then the tens.</p>  <p>$23 + 15 = 38$</p>	<p>$23 \text{ and } 15 = 38$</p> <p>I know that 3 and 5 is 8, and 20 and 10 is 30. $30 + 8 = 38$</p> $\begin{array}{r} 23 \\ + 15 \\ \hline 38 \end{array}$
<p>Adding two digit numbers— with regrouping</p>	<p>Use ten dienes, spotting the 'Sneaky ten'. Swap tens ones for a tens stick.</p> <p>$26 + 29 = 55$</p> 	<p>Draw a tens and ones grid, draw the sticks and dots to represent tens and ones. Spot the 'Sneaky Ten' and swap tens ones for a ten stick.</p> <p>$26 + 29 = 55$</p> 	<p>Column method.</p> $\begin{array}{r} 26 \\ + 29 \\ \hline 55 \\ 1 \end{array}$ <p>Add the ones. One ten to carry over to the tens column. Add the tens, including the carry over.</p>